

# A New Key Management Scheme for a User Hierarchy based on a Hybrid Cryptosystem

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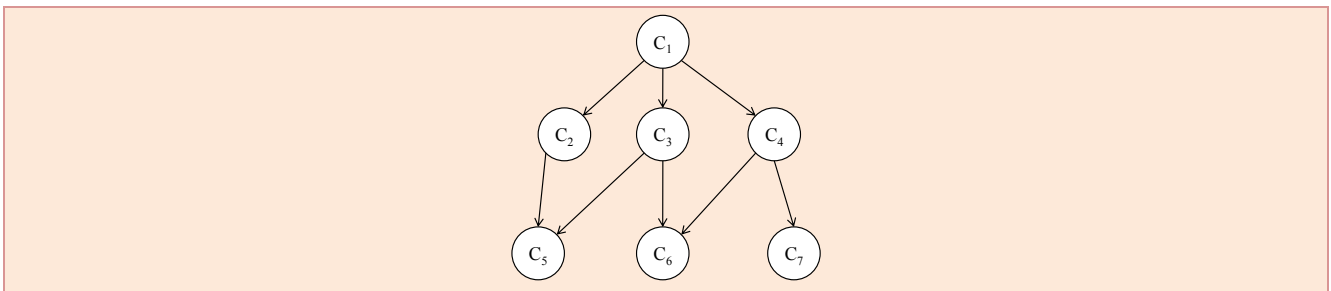
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**Abstract:** In general applications, changing a secret key of a user provides maximum security for the system. Thus, a user in an organization needs to change his/her secret key from time to time to achieve maximum security. Changing the secret key of a user in an organization is more frequent than a user simply joining or leaving the organization. Dynamic properties such as changing the key of a user in a hierarchy affects the performance of an access control scheme more than other dynamic properties such as adding or deleting a security class to the hierarchy. As a result, we need to design an effective access control scheme to change keys of users in the hierarchy. However, most schemes proposed in the literature do not provide an efficient solution. In this paper, we propose a new key management mechanism for hierarchical access control that provides an effective solution. Moreover, our scheme efficiently supports other dynamic properties, such as adding or deleting a security class. Further, we proposed an efficient procedure for key generation and key derivation for access control. Through formal and informal security analysis, we prove our scheme tolerates various known attacks in access control. We show that our scheme has better performance compared to other related schemes. As a result, higher security along with efficient access control properties makes our scheme more suitable for practical applications.

**Keywords:** Changing secret key, hierarchical access control, digital signature, one-way hash function, security

## Introduction

User hierarchy is a critical issue in access control policy for information protection systems. Since the computer communication system tends to be increasingly complicated, computer cryptography and information security obviously become more important than ever before. The rapid growth of computer networks and technology constructs a favorable environment that can tolerate multi-users in a hierarchy, which makes sharing resources unavoidable. Both industrial and academic fields have serious concerns about protecting information security from unauthorized users. Within this user hierarchy structure, a user is allowed to access all of the files of users at lower levels in the hierarchy. A hierarchy is a natural way of organizing users to reflect authority and responsibility. High-level users inherit all privileges of, and access to, users below them. The top level user possesses the greatest authority, and the bottom level user has the least authority.



**Figure 1.** An example of a POSET hierarchy

Users are divided into disjoint security classes according to their privileges. A set of  $N$  disjoint security classes, say  $C$ , where  $C = \{C_1, C_2, \dots, C_N\}$  forms a partially ordered set (POSET) with respect to a binary relation " $\leq$ ".  $C_j \leq C_i$  means the security level of the class  $C_i$  is higher or equal to the security level of the class  $C_j$ , and we call security class  $C_i$  the predecessor of security class  $C_j$ , and security class  $C_j$  a successor of security class  $C_i$ . Let this relation be denoted by  $(C_i, C_j) \in R_{i,j}$ . The hierarchy is managed by a trusted central authority (CA), which can initialize all the parameters in the hierarchy according to defined user privileges and which constructs public parameters corresponding to each user in the hierarchy in order to distribute secret keys  $SK_i$ 's to the authorized security class  $C_i$  and declares corresponding public information. In a hierarchy, a predecessor security class  $C_i$  can always derive its successor's secret key,  $SK_j$ , so that the information encrypted by  $SK_j$  by the successor security class  $C_j$  (lower than security class  $C_i$ ) can be decrypted by security class  $C_i$  using the derived secret key,  $SK_j$ , of the class  $C_j$ . Thus,  $C_i$  is able to retrieve information of  $C_j$ . For example, consider a POSET hierarchy shown in Figure 1. In this figure, we have the following relationships:  $\{C_1 \leq C_1, C_2 \leq C_1, C_3 \leq C_1, C_4 \leq C_1, C_5 \leq C_1, C_6 \leq C_1, C_7 \leq C_1\}$ ;  $\{C_2 \leq C_2, C_5 \leq C_2\}$ ,  $\{C_3 \leq C_3, C_5 \leq C_3, C_6 \leq C_3\}$ ;  $\{C_4 \leq C_4, C_6 \leq C_4, C_7 \leq C_4\}$ ;  $\{C_5 \leq C_5\}$ ;  $\{C_6 \leq C_6\}$ ; and  $\{C_7 \leq C_7\}$ . The naive solution is that security class  $C_1$  needs to store secret keys  $SK_2, SK_3, SK_4, SK_5, SK_6, SK_7$  and its own secret key,  $SK_1$ . In the same way, other security classes  $C_2, C_3, C_4$  need to store keys for their successors, too. In practical applications, each security class will have a large number of successors, and storing the corresponding keys leads to huge storage overhead and insecurity from storing the keys. This requires design of an efficient dynamic access control scheme to manage secret keys in the hierarchy.

## Review of the Previous Works

Akl and Taylor [1] first proposed the concept of a cryptographic key assignment scheme in a general POSET hierarchy based on integer factorization. As pointed out by Wang and Laih [2], Akl and Taylor's scheme is inflexible because all keys are related in a generally dependent manner, and it is not easy to adjust the hierarchy. In addition, it is hard to update a key without reassigning a lot of other keys in the hierarchy. Later, Harn and Lin [3] proposed an improvement on Akl and Taylor's scheme. However, when there are many security classes in the hierarchy, Harn and Lin [3] require a large amount of storage space due to a large number of public parameters, as explained by Hwang and Yang [4]. Harn and Lin's scheme reduces the required storage space for the public parameters in the system as compared to the Akl-Taylor scheme. After that, Wang and Laih [5] showed that Hwang and Yang's scheme is vulnerable to the collusion attack, where some security classes conspire to derive the secret keys of other leaf security classes. Recently, Lo et al. [6] proposed a key management scheme for a large leaf class hierarchy based on a public key cryptosystem. However, if the hierarchy consists of a large

number of leaf security classes with more than one parent, Lo et al.'s scheme needs to generate a large number of primes. Wong et al. [21] proposed a secure group communications protocol using key graphs. Their scheme provides three rekeying strategies and the group key management service, using any of these three rekeying strategies. Their scheme is also scalable to large groups with frequently joining and leaving of members.

Many cryptographic solutions have been proposed in the literature to solve the hierarchical access control problem efficiently. Sandhu [7] proposed a scheme for a tree hierarchy based on one-way hash function. However, it is not applicable to a general hierarchy. Yang and Li [8] proposed an access control scheme for a general hierarchy based on a one-way hash function. Chung et al. [9] proposed an efficient solution for a key management scheme. However, Das et al. [10] pointed out a security flaw in Chung et al.'s scheme, where an attacker who is not a user in any security class in the user hierarchy can derive the secret key of a security class by using the exterior root finding attack. They also proposed an improvement on Chung et al.'s scheme to remedy this serious security flaw. In recent years, several key management schemes have been proposed for a general hierarchy [11] [12] [13] [14] [15] [16]. However, these schemes do not provide an efficient solution to the dynamic key change property in a hierarchy.

Based on the literature survey, we list the following parameters to evaluate the effectiveness of cryptographic key assignment schemes in a POSET hierarchy:

- Effort needed to change a secret key of a security class in the hierarchy.
- Effort needed to update the hierarchy when a modification occurs.
- Size of secret keys and the storage space required for public parameters.
- Effort needed to compute key generation and key derivation.
- Guarantee of computational security.

## Our Contributions

In this paper, we propose a new hybrid key management mechanism for a hierarchical access control scheme, which is based on RSA and symmetric key cryptosystem and provides an efficient solution to the dynamic key change property. Moreover, our scheme efficiently supports other dynamic properties such as adding and deleting a security class.

- Our scheme provides authentication and confidentiality for the secret key of a security class.
- Our scheme provides an effective and efficient solution to the problem of changing a secret key without affecting the public data of other security classes.
- The time complexity of both the key generation and the key derivation is  $O(1)$ .
- Since changing a secret key provides maximum security for the user in a hierarchy, our scheme is more suitable for practical applications.
- Through formal and informal security analysis, we show that our scheme is secure against possible known attacks.
- Our scheme has better performance as compared to other related existing schemes.

The remainder of this paper is organized as follows. In Section 2, we propose our access control scheme. Section 3 describes the solution to the dynamic access control problems in the hierarchy. In Section 4, we perform security analysis of our proposed scheme. In Section 5, we prove the correctness of the key derivation phase and thoroughly analyze storage overhead and computational overhead. We compare the computational cost and performance analysis of our scheme with the closely related existing schemes in Section 6. Finally, we conclude the paper in Section 7.

## Our Proposed Access Control Scheme

We assume a set of  $N$  security classes, say  $C = \{C_1, C_2, \dots, C_N\}$  which forms a POSET hierarchy with the partially ordered relation " $\leq$ ". The central authority first sets up its own public and private parameters. The CA constructs a hierarchy of the POSET  $(C, \leq)$  and it assigns secret key  $SK_i$  to each security class  $C_i$  in the POSET hierarchy. In the key derivation phase, we explain the process of deriving a secret key of a successor security class in a hierarchy. We use the secure one-way hash function  $H(\cdot)$  (for example SHA-1 [18]) and the symmetric key encryption/decryption  $E(\cdot)/D(\cdot)$  (for example AES-128 [17]). Note that the AES-128 128-bit cipher-text uses a 128-bit key. SHA-1 produces a 160-bit hash value or message digest.

## ■ Set-up phase

In this phase the central authority performs the following steps.

- Step 1. The CA selects two large secret distinct primes,  $p$  and  $q$  ( $p \neq q$ ). The primes  $p$  and  $q$  could be chosen by using either the randomized Miller-Rabin primality test algorithm [19] or the deterministic AKS primality test algorithm [20].
- Step 2. The CA then computes the public parameter  $m = pq$  as the product of two generated primes  $p$  and  $q$ , and the number  $\varphi(m) = (p-1)(q-1)$  respectively, where  $\varphi(\cdot)$  is the Euler's totient or phi function [19]. Note that  $\varphi(m) = |\{a : 0 < a < m, \gcd(a, m) = 1\}|$  is the number of positive integers which are less than  $m$  and relatively co-prime to  $m$ .
- Step 3. The CA then chooses a public number  $e_{CA}$  randomly in the range  $1 < e_{CA} < m-1$  with  $\gcd(e_{CA}, \varphi(m)) = 1$ , and computes the secret number  $d_{CA}$  such that  $e_{CA}d_{CA} \equiv 1 \pmod{\varphi(m)}$ ; that is,  $d_{CA} = e_{CA}^{-1} \pmod{\varphi(m)}$ .
- Step 4. The CA finally removes the primes  $p$  and  $q$ , keeps secret the pair  $(d_{CA}, \varphi(m))$  at the CA, and publishes the pair  $(e_{CA}, m)$  on the authenticated public domain.

## ■ Hierarchy construction phase

In this phase, the CA constructs a user hierarchy according to the user privileges in the set of security classes  $C$  such that  $(C, \leq)$  forms a POSET. The following are steps needed to complete this phase successfully:

- Step 1. For each security class  $C_i$ , the CA chooses a secret number  $s_i$  of 128 bits.
- Step 2. The CA computes sub-secret key  $K_i$  as  $K_i = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_i)$  for each security class  $C_i$  in the hierarchy, where  $ID_i$  is the unique identity of the security class  $C_i$  assigned by the CA.
- Step 3. For each security class  $C_i$ , the CA computes the public parameter  $M_{i,j}$  as  $M_{i,j} = E_{K_i}(s_j)$  for all  $C_j$ , where  $(C_i, C_j) \in R_{i,j}$ .
- Step 4. The CA then sends the sub-secret key  $K_i$  to each class  $C_i$  via a secure channel.
- Step 5. Finally, the CA publishes all public parameters  $M_{i,j}$  on the authenticated public domain. The CA then removes the sub-secret keys  $K_i$  and the secret numbers  $s_i$  for security reasons.

**Example 1.** Consider the hierarchy shown in Figure 1. According to the user privileges, the CA constructs the cryptographic relationships among all security classes in the hierarchy. First, the CA chooses secret numbers  $s_1, s_2, s_3, s_4, s_5, s_6,$  and  $s_7$  for the security classes  $C_1, C_2, C_3, C_4, C_5, C_6,$  and  $C_7$  respectively. After that, the CA computes the sub-secret key  $K_i$  and public parameters  $M_{i,j}$  for each security class  $C_i$ , where  $(C_i, C_j) \in R_{i,j}$  as follows:

- C<sub>1</sub>:** CA computes sub-secret key  $K_1 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_1)$  and then public parameters  $M_{1,1} = E_{K_1}(s_1), M_{1,2} = E_{K_1}(s_2), M_{1,3} = E_{K_1}(s_3), M_{1,4} = E_{K_1}(s_4), M_{1,5} = E_{K_1}(s_5), M_{1,6} = E_{K_1}(s_6), M_{1,7} = E_{K_1}(s_7)$ .
- C<sub>2</sub>:** CA computes sub-secret key  $K_2 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_2)$  and then public parameters  $M_{2,2} = E_{K_2}(s_2), M_{2,5} = E_{K_2}(s_5)$ .
- C<sub>3</sub>:** CA computes sub-secret key  $K_3 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_3)$  and then public parameters  $M_{3,3} = E_{K_3}(s_3), M_{3,5} = E_{K_3}(s_5), M_{3,6} = E_{K_3}(s_6)$ .
- C<sub>4</sub>:** CA computes sub-secret key  $K_4 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_4)$  and then public parameters  $M_{4,4} = E_{K_4}(s_4), M_{4,6} = E_{K_4}(s_6), M_{4,7} = E_{K_4}(s_7)$ .
- C<sub>5</sub>:** CA computes sub-secret key  $K_5 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_5)$  and then public parameters  $M_{5,5} = E_{K_5}(s_5)$ .
- C<sub>6</sub>:** CA computes sub-secret key  $K_6 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_6)$  and then public parameters  $M_{6,6} = E_{K_6}(s_6)$ .
- C<sub>7</sub>:** CA computes sub-secret key  $K_7 = H(\varphi(m) \parallel d_{CA} \parallel e_{CA} \parallel ID_7)$  and then public parameters  $M_{7,7} = E_{K_7}(s_7)$ .

## ■ Key generation phase

In order to complete this phase the CA performs the following steps:

- Step 1. The CA chooses a random secret key  $SK_i$  for each security class  $C_i$  and computes the signature  $Sign_i$  of the secret key  $SK_i$  as  $Sign_i = H(e_{CA} \parallel m \parallel SK_i \parallel ID_i)$ .
- Step 2. For each security class  $C_i$ , the CA computes the public parameter  $PK_i$  as  $PK_i = [(SK_i \oplus H(Sign_i \parallel s_i \parallel ID_i)) \parallel (Sign_i)]^{d_{CA} \pmod{\varphi(m)}} \pmod{m}$  for sharing the secret key with the authorized security classes.
- Step 3. Finally, the CA removes the secret keys  $SK_i$  for security reasons. The CA then publishes the public parameters  $PK_i$  on the authenticated public domain.

**Example 2.** Reconsider the hierarchy shown in Figure 1. The CA chooses secret keys  $SK_1, SK_2, SK_3, SK_4, SK_5, SK_6$  and  $SK_7$ , and then computes the corresponding signatures  $Sign_1, Sign_2, Sign_3, Sign_4, Sign_5, Sign_6$  and  $Sign_7$  of the security classes  $C_1, C_2, C_3, C_4, C_5, C_6$  and  $C_7$ , respectively, as  $Sign_1 = H(e_{CA} \parallel m \parallel SK_1 \parallel ID_1), Sign_2 = H(e_{CA} \parallel m \parallel SK_2 \parallel ID_2), Sign_3 = H(e_{CA} \parallel m \parallel SK_3 \parallel ID_3), Sign_4 = H(e_{CA} \parallel m \parallel SK_4 \parallel ID_4), Sign_5 = H(e_{CA} \parallel m \parallel SK_5 \parallel ID_5), Sign_6 = H(e_{CA} \parallel m \parallel SK_6 \parallel ID_6)$

and  $\text{Sign}_7 = H(e_{CA} \parallel m \parallel \text{SK}_7 \parallel \text{ID}_7)$ . The CA computes the public parameters  $\text{PK}_1 = [(\text{SK}_1 \oplus H(\text{Sign}_1 \parallel s_1 \parallel \text{ID}_1)) \parallel (\text{Sign}_1)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ ,  $\text{PK}_2 = [(\text{SK}_2 \oplus H(\text{Sign}_2 \parallel s_2 \parallel \text{ID}_2)) \parallel (\text{Sign}_2)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ ,  $\text{PK}_3 = [(\text{SK}_3 \oplus H(\text{Sign}_3 \parallel s_3 \parallel \text{ID}_3)) \parallel (\text{Sign}_3)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ ,  $\text{PK}_4 = [(\text{SK}_4 \oplus H(\text{Sign}_4 \parallel s_4 \parallel \text{ID}_4)) \parallel (\text{Sign}_4)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ ,  $\text{PK}_5 = [(\text{SK}_5 \oplus H(\text{Sign}_5 \parallel s_5 \parallel \text{ID}_5)) \parallel (\text{Sign}_5)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ ,  $\text{PK}_6 = [(\text{SK}_6 \oplus H(\text{Sign}_6 \parallel s_6 \parallel \text{ID}_6)) \parallel (\text{Sign}_6)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ , and  $\text{PK}_7 = [(\text{SK}_7 \oplus H(\text{Sign}_7 \parallel s_7 \parallel \text{ID}_7)) \parallel (\text{Sign}_7)]^{d_{CA} \bmod \phi(m)} \pmod{m}$  for the security classes  $C_1, C_2, C_3, C_4, C_5, C_6,$  and  $C_7$ , respectively.

## Key derivation phase

If the security class  $C_i$  wants to derive the secret key  $\text{SK}_j$  of its successor security class  $C_j$ , where  $(C_i, C_j) \in R_{ij}$ ,  $C_i$  needs to execute the following steps:

- Step1. The security class  $C_i$  derives the secret number  $s_j$  using its own sub-secret key  $K_i$  as  $s_j' = D_{K_i}(M_{i,j})$  and then derives  $[(\text{SK}_j \oplus H(\text{Sign}_j \parallel s_j \parallel \text{ID}_j)) \parallel (\text{Sign}_j)]$  as  $[(\text{SK}_j \oplus H(\text{Sign}_j \parallel s_j \parallel \text{ID}_j)) \parallel (\text{Sign}_j)] = \text{PK}_j^{e_{CA}} \pmod{m}$ .
- Step2. The security class  $C_i$  then computes the hash value  $H(\text{Sign}_j \parallel s_j' \parallel \text{ID}_j)$  using derived secret number  $s_j'$  in Step1 and retrieves  $\text{Sign}_j$ . After that,  $C_i$  computes the secret key  $\text{SK}_j$  of the security class  $C_j$  as  $\text{SK}_j' = (\text{SK}_j \oplus H(\text{Sign}_j \parallel s_j \parallel \text{ID}_j)) \oplus H(\text{Sign}_j \parallel s_j' \parallel \text{ID}_j)$ . The CA further computes  $H(e_{CA} \parallel m \parallel \text{SK}_j' \parallel \text{ID}_j)$  using the public  $e_{CA}$ ,  $m$  and  $\text{ID}_j$ , and the derived secret key  $\text{SK}_j'$ . The CA then verifies whether the condition  $\text{Sign}_j = H(e_{CA} \parallel m \parallel \text{SK}_j' \parallel \text{ID}_j)$  holds. If it holds,  $C_i$  confirms that the derived secret key  $\text{SK}_j$  is the legitimate secret key of  $C_j$ .

## Solution to Dynamic Access Control Problem

In this section, we show that our scheme can efficiently support dynamic key management problems, including inserting a new security class into the hierarchy, deleting an existing security class, and changing the secret key of a security class.

### Inserting a new security class into the hierarchy

Let a new security class  $C_x$  with the relationships  $C_j \leq C_x \leq C_i$  be added into an existing user hierarchy. The CA executes the following steps in order to manage the access priority of  $C_x$  in the hierarchy:

- Step 1. For the security class  $C_x$ , the CA chooses a random secret number  $s_x$  of 128 bits.
- Step 2. The CA computes the sub-secret key  $K_x$  as  $K_x = H(\phi(m) \parallel d_{CA} \parallel e_{CA} \parallel \text{ID}_x)$  for the security class  $C_x$ .
- Step 3. The CA computes public parameters  $M_{x,y}$  for the security class  $C_x$  as  $M_{x,y} = E_{K_x}(s_y)$  for all  $C_y$ , where  $(C_x, C_y) \in R_{x,y}$  and public parameters  $M_{p,x}$  for each predecessor class  $C_p$  of  $C_x$  as  $M_{p,x} = E_{K_p}(s_x)$ , where  $(C_p, C_x) \in R_{p,x}$ .
- Step 4. The CA then sends the sub-secret key  $K_x$  for security class  $C_x$  via secure channel.
- Step 5. The CA chooses a random secret key  $\text{SK}_x$  for security class  $C_x$  and computes the signature  $\text{Sign}_x$  of secret key  $\text{SK}_x$  as  $\text{Sign}_x = H(e_{CA} \parallel m \parallel \text{SK}_x \parallel \text{ID}_x)$ . The CA then computes public parameter  $\text{PK}_x$  as  $\text{PK}_x = [(\text{SK}_x \oplus H(\text{Sign}_x \parallel s_x \parallel \text{ID}_x)) \parallel (\text{Sign}_x)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ .
- Step 6. Finally, the CA removes secret key  $\text{SK}_x$  and secret number  $s_x$  for security reasons. The CA then publishes the public parameters  $\text{PK}_x$ ,  $M_{x,y}$  and  $M_{p,x}$  on the authenticated public domain.

**Example 3.** Let a new security class  $C_8$  be inserted into the user hierarchy given in Figure 1 such that  $C_5 \leq C_8 \leq C_3$ . The resulting hierarchy is shown in Figure 2. The CA first chooses the secret number  $s_8$  and computes the public parameters for the predecessor security classes  $C_3$  and  $C_1$  of security class  $C_8$  as  $M_{3,8} = E_{K_3}(s_8)$  and  $M_{1,8} = E_{K_1}(s_8)$ , respectively, and the public parameter for security class  $C_8$  as  $M_{8,5} = E_{K_8}(s_5)$  where  $(C_8, C_5) \in R_{5,8}$ . The CA chooses secret key  $\text{SK}_8$  of security class  $C_8$  and computes signature  $\text{Sign}_8$  for secret key  $\text{SK}_8$  as  $\text{Sign}_8 = H(e_{CA} \parallel m \parallel \text{SK}_8 \parallel \text{ID}_8)$  and then computes the public parameter  $\text{PK}_8$  as  $\text{PK}_8 = [(\text{SK}_8 \oplus H(\text{Sign}_8 \parallel s_8 \parallel \text{ID}_8)) \parallel (\text{Sign}_8)]^{d_{CA} \bmod \phi(m)} \pmod{m}$ . Finally, the CA removes secret number  $s_8$  and secret key  $\text{SK}_8$ , and publishes public information  $M_{3,8}$ ,  $M_{1,8}$ ,  $M_{8,5}$  and  $\text{PK}_8$  on the authenticated public domain.

### Deleting an existing security class from the hierarchy

Assume that an existing security class  $C_y$  must be deleted from the user hierarchy such that the relationship  $C_j \leq C_y \leq C_i$  breaks up. The CA updates the access link of the security class  $C_y$  to terminate the access privileges of  $C_y$  over its successor. The CA performs the following steps in order to maintain the forward security of the successor classes:

- Step 1. The CA removes all the parameters corresponding to the security class  $C_y$ .
- Step 2. The CA renews secret number  $s_c$  and secret key  $SK_c$  for each successor security class  $C_c (\neq C_y)$  of the deleted security class  $C_y$ .
- Step 3. The CA recomputes public parameters  $M_{p,c}$  to all the predecessors of each successor security class  $C_c (\neq C_y)$  of deleted security class  $C_y$ . The CA then updates public parameter  $PK_c$  of each successor security class  $C_c$  of  $C_y$  with renewed secret number  $s_c$  and secret key  $SK_c$ .
- Step 4. Finally, the CA publishes the public parameter on the authenticated public domain, and deletes all secret numbers  $s_c$  and secret keys  $SK_c$  for security reasons.

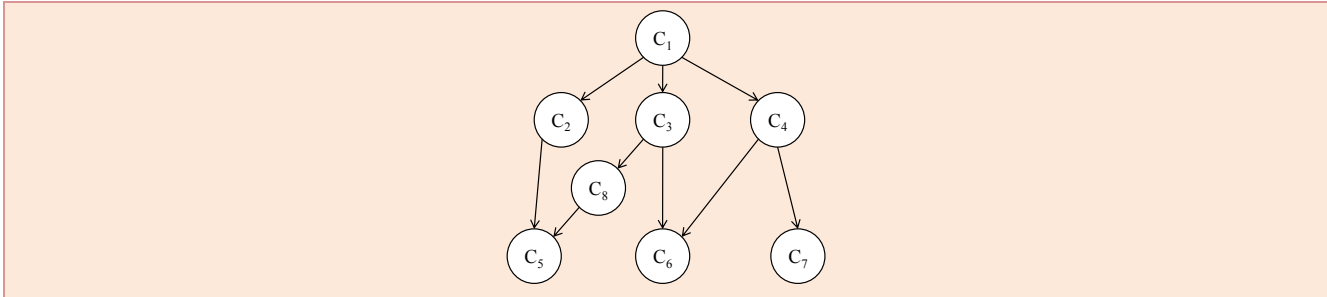


Figure 2. Hierarchy in Figure 1 after adding a new security class  $C_8$

**Example 4.** Assume that existing security class  $C_3$  is deleted from the hierarchy given in Figure 2; the resulting hierarchy is shown in Figure 3. The CA updates the hierarchy as follows: the CA reselects secret numbers  $s_8, s_6$  and  $s_5$ , the secret keys  $SK_8, SK_6$  and  $SK_5$  of the successor security classes  $C_8, C_6$  and  $C_5$  of deleted security class  $C_3$  as  $s'_8, s'_6$  and  $s'_5$  for secret keys  $SK'_8, SK'_6$  and  $SK'_5$ , respectively. The CA then recomputes the public parameters as  $M_{1,8} = E_{K_1}(s'_8), M_{1,6} = E_{K_1}(s'_6), M_{1,5} = E_{K_1}(s'_5)$ , and  $M_{2,5} = E_{K_2}(s'_5)$  with the newly generated secret numbers  $s'_8, s'_6$  and  $s'_5$ , respectively. Further, the CA computes the signatures on renewed secret keys  $SK'_8, SK'_6$  and  $SK'_5$  as  $Sign'_8 = H(e_{CA} || m || SK'_8 || ID_8), Sign'_6 = H(e_{CA} || m || SK'_6 || ID_6)$  and  $Sign'_5 = H(e_{CA} || m || SK'_5 || ID_5)$ , respectively, and then computes the public parameters  $PK_8, PK_6$  and  $PK_5$  as  $PK_8 = [SK'_8 \oplus H(Sign'_8 || s'_8 || ID_8) || Sign'_8]^{d_{CA} \bmod \phi(m)} \pmod m, PK_6 = [SK'_6 \oplus H(Sign'_6 || s'_6 || ID_8) || Sign'_6]^{d_{CA} \bmod \phi(m)} \pmod m$ , and  $PK_5 = [SK'_5 \oplus H(Sign'_5 || s'_5 || ID_8) || Sign'_5]^{d_{CA} \bmod \phi(m)} \pmod m$  for security classes  $C_8, C_6$  and  $C_5$ , respectively. The CA declares public parameters  $M_{1,8}, M_{1,6}, M_{1,5}, M_{2,5}, PK_8, PK_6$  and  $PK_5$  on the authenticated public domain and removes the secret numbers  $s'_8, s'_6, s'_5$  and secret keys  $SK'_8, SK'_6, SK'_5$  for security reasons.

### Changing secret key of a security class in the hierarchy

Let security class  $C_i$  change its secret key,  $SK_i$ , for security reasons. The CA needs to update the corresponding public parameter  $PK_i$ . The CA generates a random secret key, say  $SK'_i$ , and then computes its signature  $Sign'_i$  as  $Sign'_i = H(e_{CA} || m || SK'_i || ID_i)$  and then computes public parameter  $PK'_i$  as  $PK'_i = [(SK'_i \oplus H(Sign'_i || s_i || ID_i)) || (Sign'_i)]^{d_{CA} \bmod \phi(m)} \pmod m$ . Note that except for public parameter  $PK_i$ , all public data remains is unchanged in our scheme.

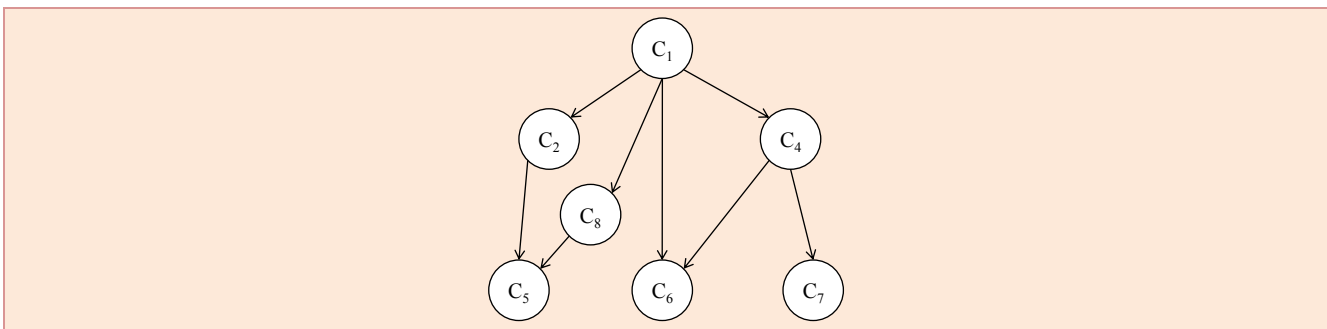


Figure 3. Hierarchy after deleting an existing security class  $C_3$  in Figure 2

**Example 5.** Consider the hierarchy given in Figure 2. Suppose the security class  $C_3$  wants to change its secret key  $SK_3$ . The CA generates a new secret key,  $SK'_3$ , and computes its signature  $Sign'_3$  as  $Sign'_3 = H(e_{CA} || m || SK'_3 || ID_3)$  and then computes the corresponding public parameter  $PK'_3$  as  $PK'_3 = [SK'_3 \oplus H(Sign'_3 || s_3 || ID_3) || Sign'_3]^{d_{CA} \bmod \phi(m)} \pmod{m}$ . The other public parameters remain unchanged.

## Security Analysis of the Proposed Scheme

In this section we show that our scheme has the ability to tolerate the following known attacks required to design an idle access control scheme.

### ■ Contrary attack

In the contrary attack, a successor security class  $C_j$ , being an insider attacker, tries to derive the secret key  $SK_i$  of its predecessor security class  $C_i$  using the available public parameters and sub-secret key  $K_j$ . Note that in our scheme,  $C_j$  first needs to decrypt the public parameter  $M_{i,j}$ , where  $(C_i, C_j) \in R_{i,j}$  in order to retrieve secret number  $s_i$  of security class  $C_i$ . After that,  $C_j$  computes secret key  $SK_i$  of predecessor security class  $C_i$ , but the task of decrypting  $M_{i,j}$  without knowing the sub-secret key  $K_i$  of security class  $C_i$  is a computationally infeasible problem. Further, solving  $PK_i$  without the secret number  $s_i$  is again a computationally infeasible problem. Therefore, our scheme is secure against this attack.

### ■ Interior collecting attack

In this attack, a successor subordinated to  $n$  parents, say  $C_i, C_{i+1}, \dots, C_{i+n-1}$  tries to derive the secret key by collecting available public parameters. Since both the symmetric-key cryptosystem (AES-128) and hash function (SHA1) behave like random oracles, the task of deriving the secret number and then the secret key becomes a computationally infeasible problem. Hence, our scheme is secure against this attack.

### ■ Exterior collecting attack

In this attack, an external attacker tries to derive/compute the secret key from a lower level security class using the available public parameters in the authenticated public domain. However, due to the resistant property of the symmetric-key cryptosystem and hash function  $H(\cdot)$ , it is a computationally infeasible problem for the external attacker to retrieve the secret number and then the secret key. Therefore, our scheme resists the exterior collecting attack.

### ■ Collaborative attack

Here, several successor security classes,  $C_j$ , launch an attack in order to derive the secret key of its predecessor security class  $C_i$ . However, the security classes  $C_j$  require symmetric-key decryption to retrieve the secret number of  $C_i$  and then secret key  $SK_i$ . However, these are again computationally infeasible problems due to one-way and collision-resistant properties of the hash function  $H(\cdot)$ . As a result, our scheme is secure against this attack.

### ■ Forward security of successors while changing $C_j < C_x < C_i$ to $C_j < C_i$

Assume that the relationship  $C_j < C_x < C_i$  is modified to another relationship  $C_j < C_i$  after removing security class  $C_x$  from the hierarchy. In our scheme, the CA not only deletes the security class  $C_x$ , but it also updates the accessibility link relationship between classes  $C_i$  and  $C_j$ , removing all public parameters associated with  $C_x$ . Further, the CA renews secret number  $s_j$  and secret key  $SK_j$  and also updates the corresponding public parameters. Thus, the authority of security class  $C_x$  over  $C_j$  completely terminates, so that  $C_x$  will not have any further ability to retrieve the updated secret key  $SK_j$  of security class  $C_j$ . Therefore, the forward security of  $C_j$  is retained, and as a result, our scheme has the ability to preserve the forward security property.

### ■ Man in the middle attack

In a man in the middle attack, a malicious user can masquerade as the CA and publish some planned public parameters  $M_{i,j}$  or  $PK_i$  on the authenticated public domain. Let a security class  $C_i$  use these public parameters to compute the secret key  $SK_j$  of its successor security class  $C_j$ . From our key derivation phase described in Section 2.4, note that security class  $C_i$  further computes the signature on the computed secret key  $SK_j$  and then verifies whether the computed signature matches the corresponding original signature  $Sign_j$ . If there is a mismatch, it suggests some attacker has changed the public data in the public domain. Usually, the public domain is considered write-protected. However, if an attacker has even the ability to update the public data in the public domain, the attacker will not be successful in changing the public data. Furthermore, the insider cannot change public data  $PK_i$  correctly without having private key  $d_{CA}$  of the CA, which is kept secret by the central authority. This is because our scheme provides the digital signature and the authentication mechanisms on secret keys in order to avoid such an attack. Hence, our scheme is also secure against the masquerade attack.

## ■ Formal security analysis of the proposed scheme

The following two formal definitions of indistinguishability of encryption–chosen plaintext attack (IND–CPA) and hash function, defined for the purpose of providing security for our new scheme in the following theorem.

**Definition 1: IND–CPA** Wu and Chen [16] describe IND and CPA as follows: Let  $SE/ME$  be the single/multiple eavesdropper and  $O_{n_1}, O_{n_2}, \dots, O_{n_N}$  be  $N$  different encryption oracles associated with secret keys  $n_1, n_2, \dots, n_N$ . We define the advantage functions of  $SE$  and  $ME$  to be:  $Adv_{\Omega, SE}^{IND-CPA}(l) = 2Pr [SE \leftarrow O_{n_1}; (m_0, m_1 \leftarrow_R SE); \theta \leftarrow_R \{0, 1\}; \gamma \leftarrow_R O_{n_1}(m_0): SE(\gamma) = \theta] - 1$ , and  $Adv_{\Omega, ME}^{IND-CPA}(l) = 2Pr [ME \leftarrow O_{n_1}, O_{n_2}, \dots, O_{n_N}; (m_0, m_1 \leftarrow_R ME); \theta \leftarrow_R \{0, 1\}; \gamma_1 \leftarrow_R O_{n_1}(m_0), \gamma_2 \leftarrow_R O_{n_2}(m_0), \dots, \gamma_N \leftarrow_R O_{n_N}(m_0): ME(\gamma_1, \gamma_2, \dots, \gamma_N) = \theta] - 1$ , respectively, where  $\theta \leftarrow_R \{0, 1\}$  represents that the  $\theta$  is a bit chosen randomly. Then we say the encryption scheme is IND–CPA secure in the single (multiple) eavesdropper setting if  $Adv_{\Omega, SE}^{IND-CPA}(l)$  (and respectively,  $Adv_{\Omega, ME}^{IND-CPA}(l)$ ) are negligible (in security parameter  $l$ ) for any probabilistic, polynomial time (PPT) adversary  $SE$  (and respectively,  $ME$ ).

**Definition 2: Hash function** There exists a secure one-way hash function  $H : X = \{0, 1\}^* \rightarrow Y^* = Z_p^*$  which satisfies the following requirements [19]:

- Given  $y \in Y$ , it is hard to find  $x \in X$  such that  $H(x) = y$ .
- Given  $x \in X$ , it is hard to find  $x' \in X (x' \neq x)$  such that  $H(x') = H(x)$ .
- It is hard to find  $x, x' \in X (x' \neq x)$  such that  $H(x') = H(x)$ .

**Theorem 1:** Assume that the used symmetric-key cryptosystem scheme  $\Omega$  is IND–CPA secure. Then under the assumption that the hash function  $H(\cdot)$  closely behaves like a random oracle, the proposed key management scheme is secure against an adversary deriving secret keys of any security class.

**Proof:** We follow the formal security proof of our scheme similar to that presented by Das et al. [10]. One can also follow the proof given in [22]. A hierarchical access control scheme for a POSET hierarchy is said to be secure if it is computationally infeasible for any attacker to derive the secret key of any class. For example, we choose an arbitrary security class  $C_j \in C$  whose secret key is  $K_j$ , where  $C = \{C_1, C_2, \dots, C_N\}$ . In our proof, we construct an adversary  $A$  such that it can derive the secret key  $K_j$  of  $C_j$ .

We now define the following two random oracles for the adversary  $A$ :

- **Reveal1:** This unconditionally outputs the input plaintext message  $M$  using the symmetric cryptosystem  $\Omega$  using the corresponding public parameters and given ciphertext message  $E_k(M)$ , without knowing the symmetric key  $k$ .
- **Reveal2:** This random oracle unconditionally outputs the input string  $x$  from the corresponding hash value  $y = H(x)$ .

Adversary  $A$  needs to run the following two experimental algorithms  $Exp1_{HACP,A}^{IND-CPA}$  and  $Exp2_{HACP,A}^{HASH}$  for our proposed hierarchical access control scheme, say HACP provided in Algorithm 1 and Algorithm 2, respectively.

### Algorithm 1 $Exp1_{HACP,A}^{IND-CPA}$

1. Read public parameter  $M_{i,j} = E_{K_i}(S_j)$  from the public domain.
2. Call *Reveal1* oracle on input  $M_{i,j}$ . Let  $S'_j \leftarrow Reveal1(M_{i,j})$ .
3. Read the public parameter  $PK_j$  from the public domain. Using the public key  $e_{CA}$  of the CA, compute  $PK_j^{e_{CA}} \pmod{m} = (SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j)) \parallel Sign_j$ .
4. Using the derived secret number  $S'_j$  and the signature  $Sign_j$ , compute  $H(Sign_j \parallel S'_j \parallel ID_j)$  and the secret key  $SK'_j = (SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j)) \oplus H(Sign_j \parallel S'_j \parallel ID_j)$ .



5. Compute the hash value  $H(e_{CA} \parallel m \parallel SK'_j \parallel ID_j)$  and compare it with the derived signature  $Sign_j$ . If it matches, return 1(true); else return 0 (false).

We define  $Succ_{HACP,A}^{IND-CPA} = \Pr[Exp1_{HACP,A}^{IND-CPA} = 1] - 1$ . Then the advantage function for  $Exp1_{HACP,A}^{IND-CPA}$  is defined by  $Adv_{HACP,A}^{IND-CPA}(t_1, q_{R_1}) = \max_A Succ_{HACP,A}^{IND-CPA}$ , where the maximum is taken over all  $A$  with execution time  $t_1$  and the number of queries  $q_{R_1}$  to the *Reveal1* oracle. We say that our scheme is secure against deriving the secret key  $K_j$  of any security class  $C_j$  if  $Adv_{HACP,A}^{IND-CPA}(t_1, q_{R_1}) \leq \epsilon$ , for any sufficiently small  $\epsilon > 0$ .

### Algorithm 2 $Exp2_{HACP,A}^{HASH}$

1. Read the public parameter  $PK_j$  from the public domain. Using public key  $e_{CA}$  of the CA, compute  $PK_j^{e_{CA}} \pmod{m} = (SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j)) \parallel Sign_j$ .
2. Call *Reveal2* oracle on input  $Sign_j$ . Let  $SK'_j \leftarrow Reveal2(Sign_j)$ .
3. Call *Reveal2* oracle on input  $H(Sign_j \parallel s_j \parallel ID_j)$ . Let  $Sign'_j \leftarrow Reveal2(H(Sign_j \parallel s_j \parallel ID_j))$ .
4. Check the condition  $Sign'_j = Sign_j$ . If it holds, return 1(true); else return 0 (false).

Similar to  $Succ_{HACP,A}^{IND-CPA}$ , we also define  $Succ_{HACP,A}^{HASH} = \Pr[Exp2_{HACP,A}^{HASH} = 1] - 1$ . Then the advantage function for  $Exp2_{HACP,A}^{HASH}$  becomes  $Adv_{HACP,A}^{HASH}(t_2, q_{R_2}) = \max_A Succ_{HACP,A}^{HASH}$ , where the maximum is taken over all  $A$  with execution time  $t_2$  and the number of queries  $q_{R_2}$  to the *Reveal2* oracle. Our scheme is said to be secure against deriving the secret key  $SK_j$  of any security class  $C_j$ , if  $Adv_{HACP,A}^{HASH}(t_2, q_{R_2}) \leq \epsilon$ , for any sufficiently small  $\epsilon > 0$ .

Consider the above experiment,  $Exp1_{HACP,A}^{IND-CPA}$  in Algorithm 1. If the attacker can decrypt  $M_{i,j}$  successfully without knowing the key, then he/she can derive the secret key  $SK_j$  of  $C_j$  ( $C_i > C_j$ ). However, it is a computationally infeasible problem since  $\Omega$  is IND-CPA secure given Definition 1. Since  $Adv_{\Omega,SE}^{IND-CPA}(l)$  (and respectively,  $Adv_{\Omega,ME}^{IND-CPA}(l)$ ) is negligible (in the security parameter  $l$ ) for any probabilistic, polynomial time (PPT) adversary SE (and respectively, ME), so  $Adv_{HACP,A}^{IND-CPA}(t_1, q_{R_1})$  is also negligible as it is dependent on the former.

We now consider another experiment,  $Exp2_{HACP,A}^{HASH}$  given in Algorithm 2, conducted by an adversary. If the adversary has the ability to solve the hash function problem provided in Definition 2, then the adversary can directly derive secret key  $SK_j$  of security class  $C_j$  ( $C_i > C_j$ ). Since the problem is deriving the input string from the given hash value, it is computationally infeasible to derive the secret key  $SK_j$  as the hash function  $H(\cdot)$  closely behaves like a random oracle. Thus,  $Adv_{HACP,A}^{HASH}(t_2, q_{R_2})$  is negligible. As a result, no adversary is able to derive the secret key of any security class.

## Performance Analysis of Our Scheme

In this section, we analyze the correctness of our key derivation phase, storage space and computational cost.

### ■ Correctness of key derivation phase

Theorem 2 provides the correctness proof of our key derivation phase.

**Theorem 2.** Assume that there are two security classes  $C_i$  and  $C_j$  with the relationship  $(C_i, C_j) \in R_{i,j}$  in a POSET hierarchy. The security class  $C_i$  can then derive secret key  $SK_j$  of  $C_j$  using its own sub-secret key  $K_i$  and the available public parameters in the authenticated public domain.

**Proof:** The security class  $C_i$  derives secret key  $SK_j$  of security class  $C_j$  using the sub-secret key  $K_i$  as follows:

$$\begin{aligned}
 s'_j &= D_{K_i}(M_{i,j}) \\
 (SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j)) \parallel (Sign_j) &= PK_j^{e_{CA}} \pmod{m} \\
 \text{Note that} \\
 PK_j^{e_{CA}} \pmod{m} &= \{[SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j) \parallel Sign_j]^{d_{CA} \pmod{\phi(m)}} \pmod{m}\}^{e_{CA}} \pmod{m} \\
 &= [SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j) \parallel Sign_j]^{d_{CA} e_{CA} \pmod{\phi(m)}} \pmod{m} \\
 &= SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j) \parallel Sign_j, \text{ since } d_{CA} = e_{CA}^{-1} \pmod{\phi(m)}.
 \end{aligned}$$

The bit string  $(SK_j \oplus H(Sign_j \parallel s_j \parallel ID_j)) \parallel (Sign_j)$  is assumed to be 320 bits, since the hash output of the secure hash function (for example SHA-1) is a 160-bit string and the string  $(SK_i \oplus H(Sign_j \parallel s_j \parallel ID_j)) \parallel (Sign_j)$  is a concatenation of

two strings  $(SK_j \oplus H(\text{Sign}_j \parallel s_j \parallel ID_j))$  and  $(\text{Sign}_j)$ , each 160-bit strings. Therefore, the first (left-most) 160 bits of  $PK_j^{e_{CA}}$  (mod  $m$ ) represents the string  $(SK_j \oplus H(\text{Sign}_j \parallel s_j \parallel ID_j))$  and the second (right-most) 160 bits of  $PK_j^{e_{CA}}$  (mod  $m$ ) represents the string  $(\text{Sign}_j)$ .

Now the secret key  $SK'_j$  is computed using these two strings and the derived secret number  $s'_j$  of security class  $C_j$  as  $SK'_j = (SK_j \oplus H(\text{Sign}_j \parallel s_j \parallel ID_j)) \oplus H(\text{Sign}_j \parallel s'_j \parallel ID_j)$ . The security class  $C_i$  then verifies the validity of derived secret key  $SK'_j$  as follows. If the condition  $\text{Sign}_j = H(e_{CA} \parallel m \parallel SK'_j \parallel ID_j)$  holds, the security class  $C_i$  confirms that the derived secret key  $SK'_j$  is legitimate and hence  $SK'_j = SK_j$ .

## Storage overhead

In our scheme, the CA needs to store the private key pair  $(d_{CA}, \varphi(m))$  and the public key pair  $(e_{CA}, m)$ . We consider the hierarchy with  $N$  security classes, say  $C_1, C_2, \dots, C_N$ , and each security class  $C_i$  has  $v_i$  successors. The private storage for each security class is 128 bits to store its own sub-secret key  $K_i$ . The storage space required for the hierarchy in our scheme is  $128 \sum_{i=1}^N v_i$ , and the storage space for public parameter  $PK_i$  requires  $1024N$  bits. Therefore, the total public storage space required in our scheme is  $(128 \sum_{i=1}^N v_i + 1024N + 2048)$  bits.

## Computational overhead

Let  $T_{\text{exp}}$  and  $T_{\text{inv}}$  denote the time complexity of executing the modular exponent, modular inverse in the finite field  $GF(2^{163})$ .  $T_{\text{SHA1}}$  denotes the time complexity of hashing a 512-bit l-message block using hash function SHA-1 [18],  $T_{\text{AES}}$  denotes the time complexity of encrypting or decrypting a 128-bit message block using AES [17] with a 128-bit key, and  $T_{\text{XOR}}$  denotes the time complexity for executing a bitwise exclusive OR operation.

Our scheme requires one  $T_{\text{inv}}$  for computing private key  $d_{CA}$  of the CA and  $N \cdot T_{\text{SHA1}}$  for computing sub-secret keys of  $N$  security classes in the hierarchy, hierarchy construction requires  $\sum_{i=1}^N v_i \cdot T_{\text{AES}}$ , and the key generation phase requires  $N \cdot (T_{\text{SHA1}} + T_e + T_{\text{XOR}})$  operations, whereas the key derivation phase requires  $\sum_{i=1}^N v_i (T_e + T_{\text{AES}} + 2T_{\text{SHA1}} + T_{\text{XOR}})$  operations. The total computational complexity require for our scheme is  $2 \sum_{i=1}^N v_i \cdot T_{\text{AES}} + \sum_{i=1}^N v_i (T_e + 2T_{\text{SHA1}} + T_{\text{XOR}}) + N \cdot (T_{\text{SHA1}} + T_e + T_{\text{XOR}})$ .

## Performance Comparison with Related Schemes

In this section, we compare the performance and security of our scheme against closely related existing schemes: the Akl-Taylor scheme [1], the Harn-Lin scheme [3] and the Hwang-Yang scheme [4] because they are based on the remote secure access public key cryptosystem. In this paper, we omit other schemes for comparison purpose, since they are not based on RSA cryptosystem.

**Table 1.** The computational complexity of different phases in the related scheme

Scheme	Adding security class	Deleting security class	Changing secret key	Key generation	Key derivation
Akl-Taylor	$O(n)$	$O(n)$	Not supported	$O(n)$	$O(1)$
Harn-Lin	$O(l)$	$O(1)$	Not supported	$O(n)$	$O(1)$
Hwang-Yang	$O(1)$	$O(1)$	Not supported	$O(y)$	$O(1)$
Ours	$O(l)$	$O(l)$	$O(1)$	$O(1)$	$O(1)$

Table 1 shows five aspects of the computational complexity, which are for adding a security class, removing a security class, changing secret keys, key generation, and key derivation. The computational cost of adding a security class is required to analyze the number of security classes needed to update secret keys when a new security class is added into POSET hierarchy. The computational cost of deleting a security class is required to analyze the number of security classes needed to update secret keys when removing an existing security class from a POSET hierarchy. Changing secret keys is the most important property of a dynamic hierarchy because it affects the security of the system. From Table 1, the Akl-Taylor scheme, Harn-Lin scheme and Hwang-Yang scheme do not support the dynamic property of changing the secret key of a security class in a hierarchy. However, our proposed scheme provides an efficient solution to the key-change property. The computational complexity for both adding a security class and deleting a security class is  $O(1)$  only in Hwang-Yang's scheme. However, Wang-Laih [5] showed that Hwang-Yang's scheme is vulnerable to the collusion attack.

In Table 2, we show the functionality of different related schemes and our scheme. From this table, it is clear that our scheme efficiently solves the dynamic access problem compared to other schemes.

From Table 3, we see that our scheme provides a digital signature and also prevents active attacks such as the “man-in-the-middle” attack. Further, our scheme is secure against all possible known attacks.

**Table 2.** The Functionalities of different phases in the related schemes

Scheme	Adding security class	Deleting security class	Changing secret key
Akl-Taylor	Not supported	Not supported	Not supported
Harn-Lin	Update partial hierarchy	Update partial hierarchy	Update partial hierarchy
Hwang-Yang	Update partial hierarchy	Update partial hierarchy	Update partial hierarchy
Ours	Update partial hierarchy	Update partial hierarchy	Do not update the hierarchy

where  $n$  represents number of security class in the hierarchy,  $l$  represents levels of the hierarchy and  $y = \sum_{\text{for all } LG_i} g_i + n_a + n_t$ , where  $g_i$  is the minimum number such that  $\binom{g_i}{k} \geq h_i$ ,  $k$  is the number of primes for distinguishing leaf classes in a leaf group and  $\binom{g_i}{k}$  means the number of ways for choosing  $k$  items from  $g_i$  and  $h_i$  denotes the number of leaf classes in  $LG_i$ ,  $n_a$  denotes the number of leaf security classes that has more than one parents and  $n_t$  denotes the number of non-leaf security classes.

**Table 3.** The security comparison of related schemes

Scheme	Whether provides digital signature to the secret key	Whether prevents “man-in-the-middle” attack
Akl-Taylor	No	No
Harn-Lin	No	No
Hwang-Yang	No	No
Ours	Yes	Yes

## Conclusions

In this paper, we proposed a new key management scheme in a user hierarchy. Our scheme provides an efficient solution to the problem of changing secret keys of a security class in the hierarchy. In addition, our scheme has the ability to efficiently support other dynamic properties, such as adding a new security class to the hierarchy and deleting an existing security class from the hierarchy. Through formal security analysis as well as informal security analysis, we have shown that our scheme has the ability to tolerate known attacks. Moreover, our scheme is efficient compared with the other approaches. Considering the higher security and efficiency in solving dynamic access control problems, our scheme is more suitable for practical applications. As the applications of the proposed scheme are concerned, the proposed scheme can be also used for ad-doc communications or infrastructure communications.

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